

Chapter 13 / Example 5

Binomial probabilities

- a** In a family of six children, find
- the probability that there are exactly three girls
 - the probability that exactly three consecutive girls are born.
- b** A study shows that 0.9% of a population of over 4 000 000 carries a virus. Find the smallest size of sample from the population required in order that the probability of the sample having no carriers is less than 0.4.

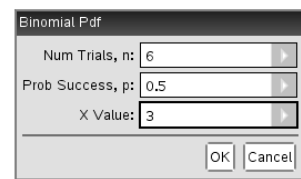
$G \sim B(6, 0.5)$. Find $P(G = 3)$.

Open a new document and add a Calculator page.

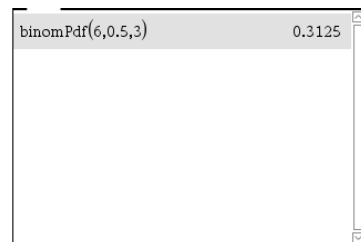
Press **menu** 5:Probability | 5:Distributions | A:Binomial Pdf...

Enter 6 as the number of trials, 0.5 as the probability of success and 3 as the X value.

Press **enter** or click OK with the touchpad.



The GDC displays the solution $P(G = 3) = 0.3125$.



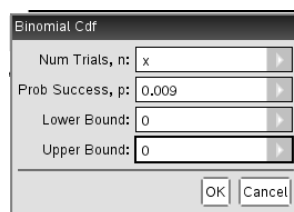
$$P(3 \text{ consecutive girls}) = 4 \times \left(\frac{1}{2}\right)^6 = 0.0625.$$

Type $f1(x)$ and press **ctrl** **⏏** **⌈:=⌋**.

Press **menu** 5:Probability | 5:Distributions | B:Binomial Cdf...

Enter x as the number of trials, 0.009 as the probability of success and 0 as the Lower Bound and 0 as the Upper Bound.

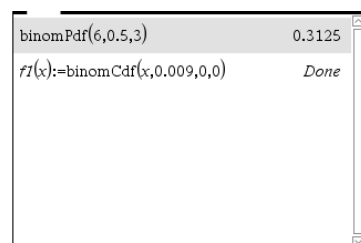
Press **enter** or click OK with the touchpad.



The function $f1(x)$ is defined.

Display this function in a table.

Press **ctrl** **doc** **(⌈+page⌋)** and add a Lists & Spreadsheet page.



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Press **ctrl** **T** to change from a spreadsheet to a table.

Press **enter**.

The GDC displays a table of $f1(x)$.

x	f1(x):=
	binomCdf(x,0.009,0,0)
1.	0.991
2.	0.982081
3.	0.973242
4.	0.964483
5.	0.955803

Scroll down the table using **▼**.

From the table, you can see that $n = 102$ is the first value for which $P(C = 0) < 0.4$.

Hence $n = 102$ is the minimum value required.

x	f1(x):=
	binomCdf(x,0.009,0,0)
100.	0.404916
101.	0.401272
102.	0.397661
103.	0.394082
104.	0.390535